THE WEST AFRICAN EXAMINATIONS COUNCIL
West African Senior School Certificate Examination
May/June 2013
MATHEMATICS (CORE) 1
1½ hours

Do not open this booklet until you are told to do so. While you are waiting, read and observe the following instructions carefully. Write your name and index number in the spaces provided above.

Answer all the questions on your Objective Test answer sheet.

1. Use 2B pencil throughout.
2. On the pre-printed answer sheet, check that the following details are correctly printed:
   (a) In the space marked Name, check your surname followed by your other names.
   (b) In the spaces marked Examination, Year, Subject and Paper, check ‘WASSCE May/June’, ‘2013’, ‘MATHEMATICS (CORE)’, and ‘1’ in that order.
   (c) In the box marked Index Number, your index number has been printed vertically in the spaces on the left-hand side, and each numbered space has been shaded in line with each digit. Reshade each of the shaded spaces.
   (d) In the box marked Subject Code, the digits 402112 are printed vertically in the spaces on the left-hand side. Reshade the corresponding numbered spaces as you did for your index number.
3. An example is given below. This is for a female candidate whose name is Nasadi Maku BOADI. Her index number is 7102143958 and she is offering Mathematics (Core) 1.

THE WEST AFRICAN EXAMINATIONS COUNCIL
ANSWER SHEET

PRINTED IN BLOCK LETTERS
BOADI NASADI MAKU GHA
Examination: WASSCE May/June Year: 2013
Subject: MATHEMATICS (CORE) Paper: 1

INSTRUCTIONS TO CANDIDATES
1. Use grade 2B pencil throughout.
2. Answer each question by choosing one letter and shading it like this: 
3. Erase completely any answers you wish to change.
4. Leave extra spaces blank if the answer spaces provided are more than you need.
5. Do not make any markings across the heavy black marks at the right hand edge of your answer sheet.

INDEX NUMBER

<table>
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SUBJECT CODE

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For Supervisors only
If candidate is absent
Shade this space.
Answer all the questions.

Mathematical tables may be used in any question. The use of non-programmable, silent and cordless calculator is allowed.

Each question is followed by four options lettered A to D. Find the correct option for each question and shade in pencil on your answer sheet, the answer space which bears the same letter as the option you have chosen.

Give only one answer to each question. An example is given below.

The ages, in years, of four boys are 10, 12, 14 and 18. What is the average age of the boys?
A. 12 years
B. 12½ years
C. 13 years
D. 13½ years

The correct answer is 13½ years, which is lettered D, and therefore answer space D would be shaded.

Think carefully before you shade the answer spaces; erase completely any answers you wish to change.

Do all rough work on this question paper.

Now answer the following questions:

1. Solve the equation: \(2^{(x-3)} = 8^{(3-x)}\).
   A. \(x = 3\)
   B. \(x = 2\)
   C. \(x = 1\)
   D. \(x = 0\)

2. Multiply \(6.4 \times 10^9\) by \(3.1 \times 10^3\) and leave the answer in standard form.
   A. \(1.984 \times 10^6\)
   B. \(1.984 \times 10^9\)
   C. \(1.984 \times 10^8\)
   D. \(1.984 \times 10^7\)

3. Simplify: \(6\frac{1}{3} \div (21\frac{1}{3} \times 2\frac{1}{3} - 21)\).
   A. \(6\frac{3}{4}\)
   B. 4
   C. \(\frac{3}{4}\)
   D. \(\frac{4}{3}\)

4. Express as a ratio: the speed of 1 km/min to the speed of 10 m/s.
   A. 5 : 3
   B. 5 : 4
   C. 3 : 4
   D. 3 : 5
5. If $y$ varies directly as $(2x + 3)$ and $x = 5$ when $y = 52$, what is the value of $x$ when $y = 36$?
   A. 4
   B. 3
   C. 2
   D. 1

6. If $\frac{4n}{m} = 119\frac{1}{3}$, what is the value of $m$?
   A. 4
   B. 3
   C. 2
   D. 1

7. Simplify: $\frac{1}{2}\sqrt{25} - \frac{1}{2}\sqrt{50}$
   A. $2\sqrt{2}$
   B. $\sqrt{2}$
   C. $-\sqrt{2}$
   D. $-2\sqrt{2}$

8. An agent receives $x\%$ commission on every sale on product $P$ and $y\%$ commission on every sale on product $Q$. If his total sales for a particular day were $2000$ and $7000$ for products $P$ and $Q$ respectively, what was the total commission of the agent?
   A. $\$ (70x + 40y)$
   B. $\$ (20x + 5y)$
   C. $\$ (20x + 70y)$
   D. $\$ (70x + 20y)$

9. Solve the simultaneous equations: $\frac{2u}{3} = 1$, $\frac{2u}{3} - v = 2$.
   A. $u = 6$, $v = 2$
   B. $u = 2$, $v = 6$
   C. $u = -2$, $v = 6$
   D. $u = -6$, $v = 2$

10. If $\frac{4x - 1}{2} < 2$, solve for $x$.
    A. $x < -7$
    B. $x < -17$
    C. $x > -17$
    D. $x > -7$

11. Find the smaller value of $x$ which satisfies the equation: $x \left( x + \frac{6}{x} - 1 \right) = 12$.
    A. 3
    B. 2
    C. -2
    D. -3
12. If \( R = \frac{h}{2} + \frac{d^2}{8h} \), express \( d \) in terms of \( R \) and \( h \).
   A. \( \sqrt{4h(2R-h)} \)
   B. \( \sqrt{4h(R-h)} \)
   C. \( \sqrt{4h(h-R)} \)
   D. \( \sqrt{4h(h-2R)} \)

13. The sum of two numbers is 15. One of the numbers is \( 1 \frac{1}{2} \) times the other. Find the bigger number.
   A. 6
   B. 9
   C. 10
   D. 12

14. If \( x^2 + 1 - (x - 2)(x + 1) = 0 \), find the value of \( x \).
   A. 3
   B. 1
   C. -1
   D. -3

15. The radius, \( r \), of a cone is twice its height, \( h \) (in metres). Express the volume of the cone in terms of \( h \).
   A. \( \frac{1}{3} \pi h^3 \text{ m}^3 \)
   B. \( \frac{1}{3} \pi h^2 \text{ m}^3 \)
   C. \( \frac{1}{12} \pi h^3 \text{ m}^3 \)
   D. \( \frac{2}{3} \pi h^2 \text{ m}^3 \)

16. In the diagram, \( PQ \) and \( RS \) are parallel chords of a circle of radius 5 cm. If \( |PQ| = 8 \text{ cm} \) and \( |RS| = 6 \text{ cm} \), how far apart are the chords?
   A. 3 cm
   B. 4 cm
   C. 7 cm
   D. 9 cm
17. A pyramid has a square base and its vertical height is 8 cm. If the diagonal of its base is $12\sqrt{2}$ cm, calculate its volume.
   A. 364 cm$^3$
   B. 374 cm$^3$
   C. 384 cm$^3$
   D. 398 cm$^3$

18. In the diagram, $PQRS$ is a trapezium with $/ PS /= 7$ cm, $/ QR /= 15$ cm and $/ SR /= 10$ cm.
   If $P\Sigma R = 150^\circ$ and $PS//QR$, calculate the area of the trapezium.
   A. 35 cm$^2$
   B. 55 cm$^2$
   C. 56 cm$^2$
   D. 70 cm$^2$

19. The interior angles of a hexagon are $2r$, $3r$, $2r$, $5r$, $r$ and $2r$. Find the value of $r$.
   A. 96$^\circ$
   B. 80$^\circ$
   C. 48$^\circ$
   D. 36$^\circ$

20. In the diagram, $O$ is the centre of the circle, $P\Sigma R = 108^\circ$ and $\angle ORK = 20^\circ$.
   Calculate $\angle OPK$.
   A. 27$^\circ$
   B. 34$^\circ$
   C. 36$^\circ$
   D. 42$^\circ$
21. Find the value of $x$ in the diagram.
   A. 95°
   B. 75°
   C. 55°
   D. 20°

22. Edem drew a straight line $XY$ on a plain sheet of paper. Using a pair of compasses with centre $X$ and a convenient radius, he drew an arc intersecting $XY$ at $P$. Using the same radius and $P$ as the centre, he drew another arc to intersect the first arc at $T$. He joined $T$ to $X$ and read off $\angle TXP$ with a protractor. What value did he read?
   A. 90°
   B. 75°
   C. 60°
   D. 45°

23. A bird on top of a tree 15 m high was observed at an angle of elevation of 75° from the same horizontal ground as the foot of the tree. Calculate, correct to the nearest whole number, the distance of the observer from the foot of the tree.
   A. 4 m
   B. 6 m
   C. 7 m
   D. 56 m

24. If $\tan x = \frac{1}{\sqrt{3}}$, where $0° \leq x \leq 90°$, find $(\sin x - \cos x)$
   A. $\frac{1-\sqrt{3}}{2}$
   B. $\frac{2}{1-\sqrt{3}}$
   C. $\frac{\sqrt{3}-1}{2}$
   D. $\frac{2}{\sqrt{3}-1}$

25. If the bearing of $R$ from $Q$ is 135°, find the bearing of $Q$ from $R$.
   A. 045°
   B. 225°
   C. 270°
   D. 315°
The table shows the distribution of marks scored by some students in a test. Use it to answer Questions 26 and 27.

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26. What is the median mark?
   A. 3.0
   B. 3.5
   C. 4.0
   D. 4.5

27. If two students are selected at random without replacement, what is the probability that they scored above the mode?
   A. $\frac{2}{23}$
   B. $\frac{1}{3}$
   C. $\frac{2}{3}$
   D. $\frac{16}{23}$

28. A box contains 20 identical balls. 8 of them are red, 7 white and the rest black. If two balls are chosen at random from the box without replacement, find the probability that they are both red or both white or both black.
   A. $\frac{50}{200}$
   B. $\frac{77}{200}$
   C. $\frac{50}{190}$
   D. $\frac{77}{190}$

29. Express $2 - 3\log_{10} 2$ as the logarithm of a single number.
   A. $\log_{10} \left( \frac{25}{12} \right)$
   B. $\log_{10} \left( \frac{25}{12} \right)$
   C. $\log_{10} \left( \frac{25}{4} \right)$
   D. $\log_{10} \left( \frac{25}{2} \right)$
The pie chart shows the distribution of 600 mathematics textbooks for Science, Arts, Business and Technical classes. Use it to answer Questions 30 and 31.

30. How many text books are for the technical class?
   A. 100
   B. 150
   C. 200
   D. 250

31. What percentage of the total number of textbooks belong to science class?
   A. 12 $\frac{1}{2}$%
   B. 20 $\frac{1}{2}$%
   C. 25%
   D. 41 $\frac{2}{3}$%

32. A trader took a loan of Ghs 5,500.00 from a bank and paid back Ghs 6,000.00 after 10 months. At what rate, correct to the nearest percentage, was the simple interest charged?
   A. 11%
   B. 10%
   C. 8%
   D. 7%

The diagram shows a rhombus PQRS with diagonals PR and SQ. \( |PT| = 24 \text{ cm} \) and \( |PQ| = 25 \text{ cm} \). Use this information to answer Questions 33 and 34.

33. What is the value of \( \angle PTQ \)?
   A. 45°
   B. 60°
   C. 75°
   D. 90°
34. Calculate \( ST \).
   A. 35 cm
   B. 28 cm
   C. 22 cm
   D. 7 cm

35. Which of the shaded regions in the Venn diagrams illustrates the set \( P' \cup Q' \)?

A.  

B.  

C.  

D.  

36. Calculate the product of the third and fourth terms of the sequence
   \[ T_n = 2(2 + 3^{n-1}) \]
   A. 1616
   B. 1352
   C. 1276
   D. 1160

37. Which of the following illustrates the solution of the inequality
   \[ \frac{x}{3} - \frac{(x-3)}{2} \leq 1 \] on a number line.

A.  

B.  

C.  

D.  

Turn over
38. Simplify: \( \frac{1}{x+1} - \frac{2}{x^2-1} + \frac{1}{x^2-1} \)
   A. \( \frac{x-2}{x^2-1} \)
   B. \( \frac{3x}{x^2-1} \)
   C. \( \frac{x}{x^2-1} \)
   D. \( \frac{x+1}{x^2-1} \)

39. Given that \( x = \frac{1}{2} \) and \( y = 2 \), evaluate \( (2xy)^{-\frac{1}{2}} + \frac{4}{y} \).
   A. \( 2 \frac{5}{9} \)
   B. \( 8 \frac{1}{4} \)
   C. \( 9 \frac{1}{4} \)
   D. 29

40. If the perimeter of a square is equal to the area of an equilateral triangle of side 3.2 cm, find, correct to 2 decimal places, the area of the square.
   A. \( 1.23 \) cm\(^2\)
   B. \( 1.92 \) cm\(^2\)
   C. \( 7.68 \) cm\(^2\)
   D. \( 15.36 \) cm\(^2\)

41. Factorize completely: \( m^6 - 2mn^3 + n^6 \).
   A. \( n(m - n)^3 \)
   B. \( n(m + n)^3 \)
   C. \( n(m-n)(m+n) \)
   D. \( n(m-n)(n - m) \)

42. Simplify: \( \frac{3}{x+3} - \frac{2(x-3)}{x^2-9} \).
   A. \( \frac{2}{x+3} \)
   B. \( \frac{2}{x-3} \)
   C. \( \frac{1}{x+3} \)
   D. \( \frac{1}{x-3} \)
In the diagram, $\overline{SY} || \overline{UW}$, $\overline{SV} || \overline{XW}$, $\angle SYT = 40^\circ$ and $\angle UVW = 70^\circ$. Use the diagram to answer Questions 43 and 44.

43. Find the value of $x$.
   A. $110^\circ$
   B. $95^\circ$
   C. $90^\circ$
   D. $85^\circ$

44. Find the value of $y$.
   A. $70^\circ$
   B. $85^\circ$
   C. $90^\circ$
   D. $95^\circ$

45. If $(-2, 4)$ is a point on the graph of $y = px^2 - 2x + 4$, where $p$ is a constant, find the value of $p$.
   A. 2
   B. 1
   C. $-1$
   D. $-2$

46.

The figure is made up of two semi-circles whose diameters are 14 cm and 7 cm. If $P Q = R S = \frac{31}{2}$ cm, find the perimeter of the figure.

[Take $\pi = \frac{22}{7}$]

A. 73 cm
B. 66 cm
C. 44 cm
D. 40 cm

Turn over
47. In the diagram, \( \angle ZXY = y^\circ, \angle ZYX = (y + 17)^\circ, \angle PZX = x^\circ \) and \( \angle YZT = (2x - 43)^\circ \). Find the value of \( y \).
   A. 40°
   B. 36°
   C. 20°
   D. 9°

48. Which of these triangles are congruent to each other?
   A. I, II and III
   B. I and II only
   C. II and III only
   D. I and III only

49. Two adjacent angles on a straight line are \( (x - 60)^\circ \) and \( (y + 30)^\circ \). Find the value of \( x + y \).
   A. 210°
   B. 150°
   C. 90°
   D. 30°

50. Given that \( \{x: 4.5 < x \leq 12\} \), where \( x \) is an even integer. List the values of \( x \).
   A. \{6, 8, 10, 12\}
   B. \{4, 6, 8, 10\}
   C. \{6, 8, 12\}
   D. \{4, 10, 12\}

END OF PAPER